

# The Dynamics of Policy Complexity

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# Badly-designed systems

- Excessive complexity in organizations and systems
  - \* Public policy
  - \* Organizational bureaucracies
  - \* Software development
- This paper – complexity due to:
  - \* Frictions in design process
  - \* Conflict between designers

# Kludge

## Definition

Kludge: an ad-hoc modification to an existing system that is functional but inefficient.

# Obamacare: a kludge

## US Affordable Care Act of 2010 (“Obamacare”)

- Patches over existing private insurance system
  - ▶ Individual mandate, coverage requirements, etc
- Excessive complexity due to ‘plugging gaps’ design
- Entanglement w/ existing system creates frictions:
  - ▶ Once enacted, makes existing system even more entrenched

# Kludges

Key elements of kludges:

- interdependencies
- incremental change
- external shocks (Ely 2011, Kolutilin and Li WP), or
- conflict (this paper)

# Preview

This paper: policymaking in setting of political conflict

- Focus on long-run outcome w/ myopic players
- Conflict + Interdependence  $\Rightarrow$  persistent complexity
- Complexity begets complexity:
  - \* simple policies remain simple
  - \* complex policies grow more complex

# Preview

Comparative statics: persistent complexity iff

- Strong, extremist ideological preferences
- Relatively equal political power
- Severe institutional frictions

# Preview

With non-myopic players, additional effects:

- *Intentional Complexity*: “building a moat”
- *Strategic extremism*: “shifting the goalposts”
- Lesson: increasing discount factor exacerbates kludge



## Lit review

- Kludges: Ely (2011), Kolotilin and Li (WP)
- Rule Development: Ellison and Holden (2013)
- Policy Politics: Bonatti and Rantakari (2015), Callander and Hummel (2014)

# Outline

- 1 Intro
- 2 Model**
- 3 One-Player Game
- 4 Dynamics of Conflict
- 5 Strategic Effects
- 6 Conclusion

# Model

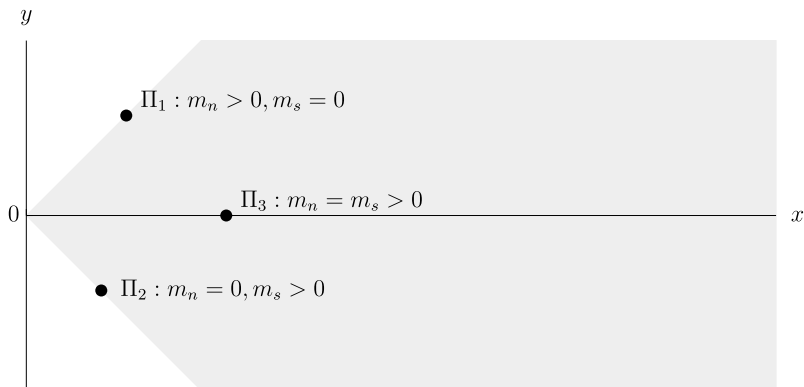
- Continuous time,  $t \geq 0$ .
- Policy  $\Pi(t)$  = continuum of infinitesimal, equal-weighted elements  $\pi$
- Each element has a direction: either northern ( $n$ ) or southern ( $s$ )
- Policy position is difference between masses of northern vs southern elements:

$$y(t) = m_n(t) - m_s(t)$$

- Policy complexity is total mass of elements:

$$x(t) = m_n(t) + m_s(t)$$

# Policy Diagram: Examples



Policy with only one type of element is *simple*  
(e.g.,  $\Pi_1$  and  $\Pi_2$ )

## Policy Preferences

- 2 players, (N)orth and (S)outh
- Each player  $I$  cares about policy complexity ( $x$ ) and position ( $y$ ):

$$V_{I,t} = \int_{\tau=t}^{\infty} e^{-\rho_I \tau} u_I(\tau) d\tau,$$
$$u_I(\tau) = -\zeta_I |y_I - y(\tau)| - x(\tau).$$

- $y_I$  is player  $I$ 's *ideal* position
- $\zeta_I$  is player  $I$ 's ideological *zeal*

$$y_N > 0, y_S < 0,$$
$$\zeta_N, \zeta_S > 1$$

## Policy Preferences

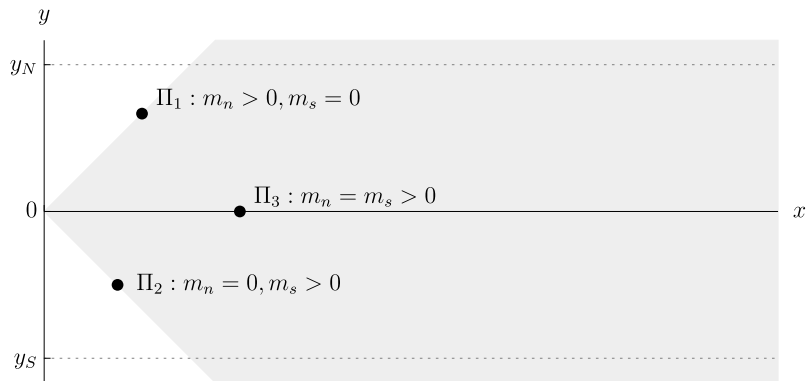
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# Policy Diagram: Preferences



# Interdependencies

- Undirected network over elements in  $\Pi(t)$
- New elements uniformly randomly form links with existing elements:
- Each new element forms  $\kappa$  links per unit mass of existing elements
- \* If element  $x$  deleted, then all direct neighbours also removed.
- Players do not observe time- $t$  network structure, but understand network formation process



# Interdependencies

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## Incremental Policymaking

- At any instant  $t$ , one player  $I(t)$  in control
  - Adds new elements  $A(t)$  and deletes  $D(t) \in \Pi(t)$
- $\Rightarrow R(t) = \{D(t) \text{ and neighbours of } D(t)\} \subseteq \Pi(t)$  removed
- Player faces flow constraint on addition and removal *rates*:

$$\frac{d}{dt}|\mathcal{A}(t)| + \frac{d}{dt}|\mathcal{R}(t)| \leq \gamma$$

where  $\mathcal{A}(t)$ ,  $\mathcal{R}(t)$  are accumulated sets of additions and removals:

$$\mathcal{A}(t) = \bigcup_0^t A(\tau), \quad \mathcal{R}(t) = \bigcup_0^t R(\tau)$$

- Constraint represents limited political resources to persuade voters, overcome interest groups, etc

# Policymaking Technology

Consider composition of removal set  $R(t)$ :

- $D(t)$ 's neighbours are representative sample of  $\Pi(t)$
- i.e.,  $n/s$  ratio in  $R(t)$  is weighted avg. of  $n/s$  ratio in  $D(t)$  and  $\Pi(t)$
- At  $\lim \kappa \rightarrow \infty$ ,  $n/s$  ratio in  $R(t)$  equals  $\frac{m_n}{m_s}$

## Reduced-Form: Policymaker's Problem

- Player  $I(t)$  chooses

$$\text{addition rates } a_n^+(t) \geq 0, a_s^+(t) \geq 0$$

$$\text{removal rates } a_n^-(t) \geq 0, a_s^-(t) \geq 0$$

- so masses of north and south elements,  $m_n$  and  $m_s$ , evolve as

$$\dot{m}_i(t) = a_i^+(t) - a_i^-(t)$$

- subject to flow constraints

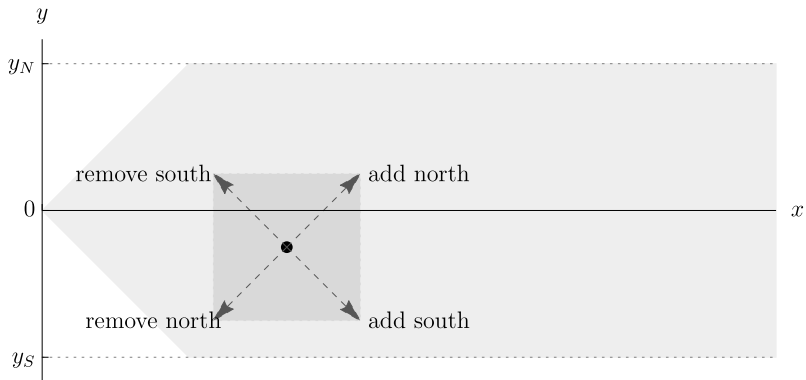
$$a_\ell^+(t) + a_r^+(t) + a_\ell^-(t) + a_r^-(t) \leq \gamma^{-1},$$

$$a_i^-(t) = 0 \text{ if } m_i(t) = 0$$

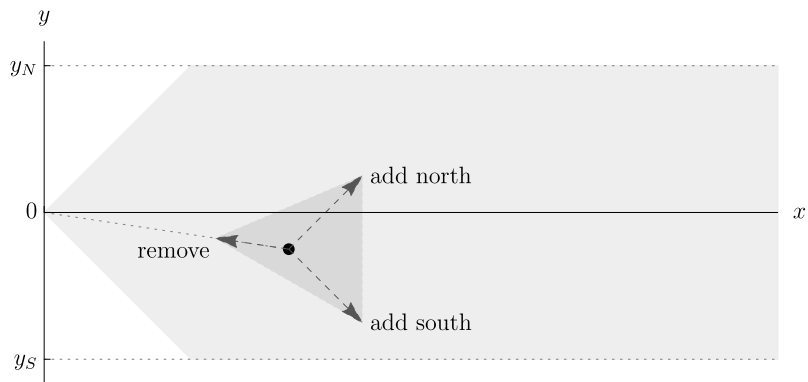
- and *entanglement constraint* (given  $\kappa \rightarrow \infty$ )

$$\frac{a_n^-(t)}{a_s^-(t)} = \frac{m_n}{m_s}$$

# Unentangled Policymaking



# Entangled Policymaking



# Dynamics

- Player  $N$  starts with control at  $t = 0$  (WLOG)
- Whenever  $I$  in control, control switches to  $-I$  at random time
- Control switch from  $I$  to  $-I$  has constant arrival rate  $\lambda_I$ .  
(i.e., power transitions independent of current policy position)
  
- Focus on myopic setting,  $r_I \rightarrow \infty$ : so
- Policymaker  $I(t)$  maximizes  $\frac{d}{dt} u_I(t)$ .

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# One-Player Game: Dynamics

Myopic player  $N$ . Focus on non-extreme policies,  $y_S \leq y \leq y_N$

## Observation

If  $(x, y)$  is  $S$ -simple, then  $N$  removes elements.

$$(a_n^+, a_s^+, a^-) = (0, 0, \gamma^{-1})$$



# One-Player Game: Dynamics

## Observation

If  $(x, y)$  is **almost**  $S$ -simple, then  $N$  removes elements.

$$(a_n^+, a_s^+, a^-) = (0, 0, \gamma^{-1})$$

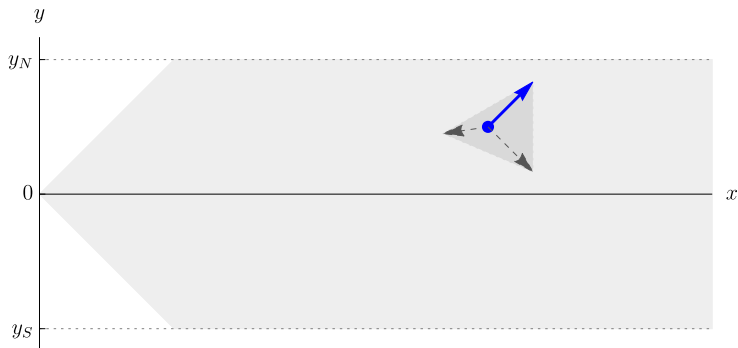


# One-Player Game: Dynamics

## Observation

*Otherwise,  $N$  adds elements towards his ideal:*

$$(a_n^+, a_s^+, a^-) = (\gamma^{-1}, 0, 0)$$



# One-Player Game: Dynamics

## Observation

*N moves along own ideal once he gets there:*

$$(a_n^+, a_s^+, a^-) = \left( \gamma^{-1} \frac{y}{x+y}, 0, \gamma^{-1} \frac{x}{x+y} \right).$$



# One-Player Game: Dynamics

## Observation

At **simple, ideal** policy,  $N$  stagnates:

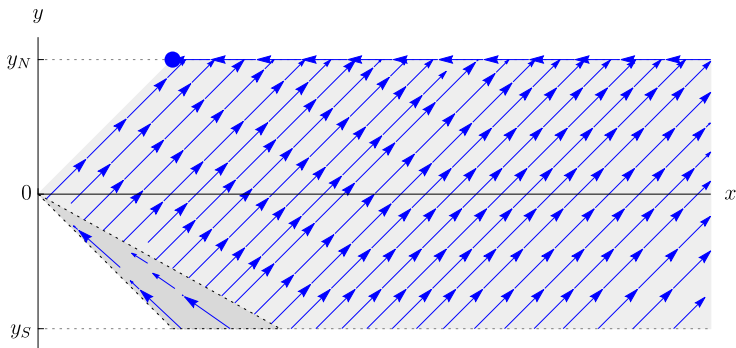
$$(a_\ell^+, a_r^+, a^-) = (0, 0, 0).$$



# One-Player Game: Dynamics

## Observation

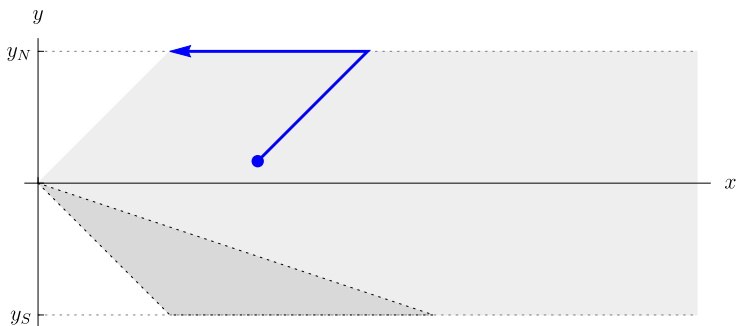
*L removes elements in "basin":  $\zeta_N < \frac{2x}{x+y}$ .  
Otherwise, he adds (or moves along ideal).*



# One-Player Game: Dynamics

## Observation

*For any starting policy  $\Pi(0)$ , simple ideal policy eventually attained.  
(i.e., no kludge without conflict.)*

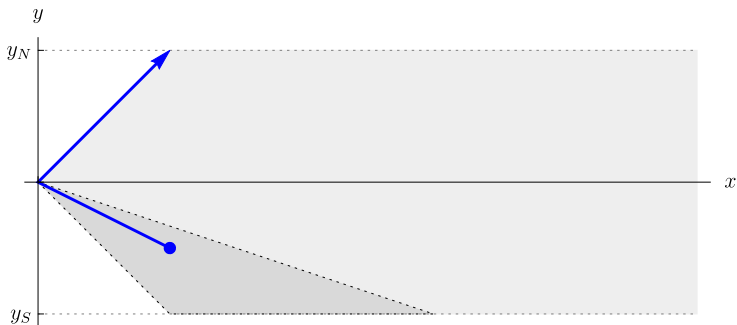




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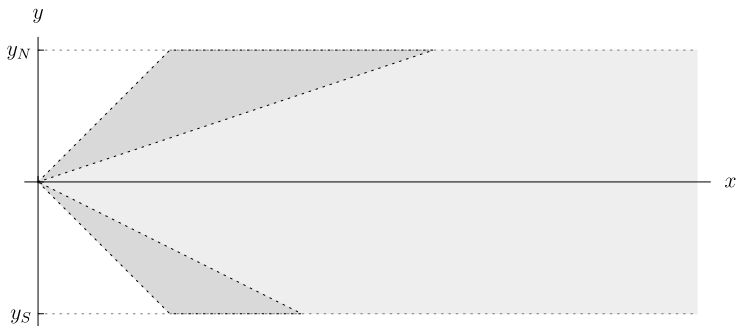


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## Two-Player Game: Preliminary Observations

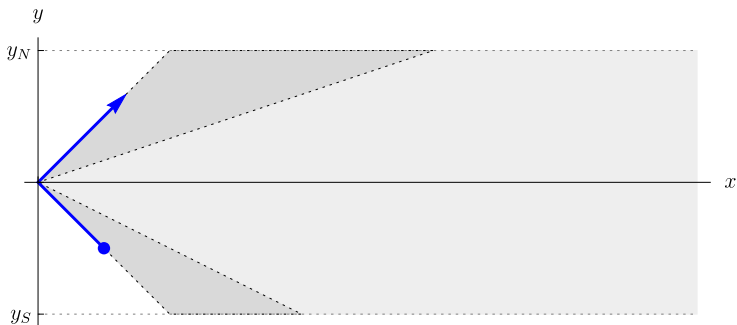
- Myopic players  $\rightarrow$  no strategic interactions;
  - Players' strategies same as in one-player game
- Can restrict attention to  $y \in [y_S, y_N]$ ;
  - Policy never becomes "extreme"



## Two-player game: persistent simplicity

### Observation

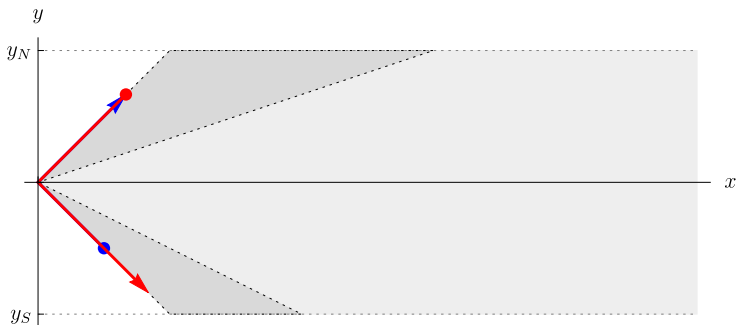
*Suppose  $\Pi(t)$  is simple. Then  $\Pi(\tau)$  will be simple for all  $t > \tau$ .*



# Two-player game: persistent simplicity

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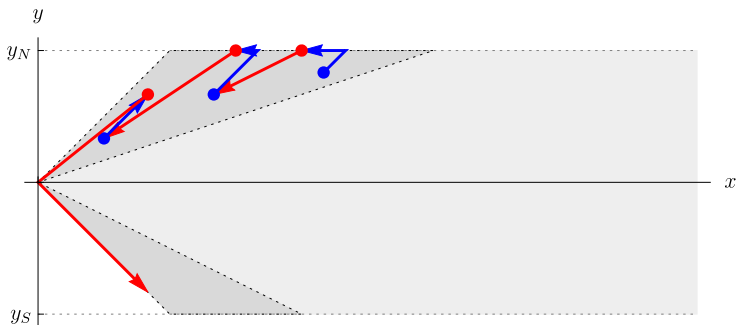
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## Two-player game: persistent simplicity

### Lemma

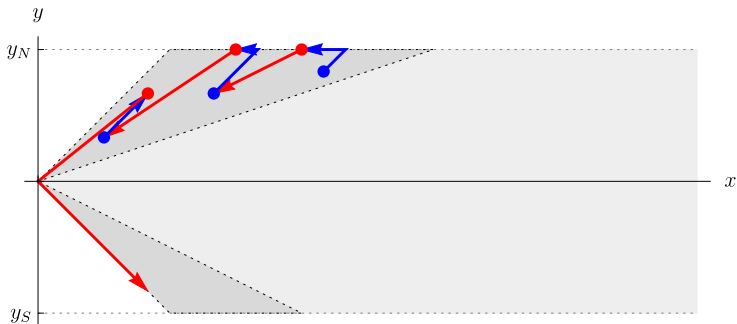
Suppose  $\Pi(t)$  is “approx. simple” ( $\frac{2x}{x+y} < \zeta_N$ , or  $\frac{2x}{y-x} < \zeta_S$ ). Then policy eventually becomes simple.



# Two-player game: persistent simplicity

## Observation

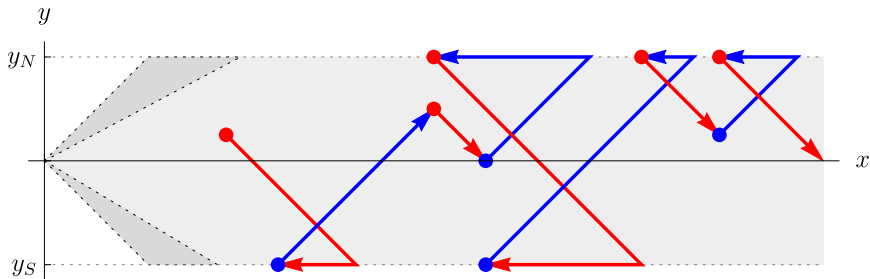
*“Approx. simple” policies are attracting basin for set of simple policies.*



# Long-run outcome: two possibilities

## Definition

If  $\lim_{t \rightarrow \infty} x(t) = \infty$ , then we say policy is kludged





## Long-run outcome: two possibilities

### Definition

*If  $\lim_{t \rightarrow \infty} x(t) = \infty$ , then we say policy is kludged*

### Lemma

*In the long-run ( $t \rightarrow \infty$ ), policy is almost surely either simple or kludged*

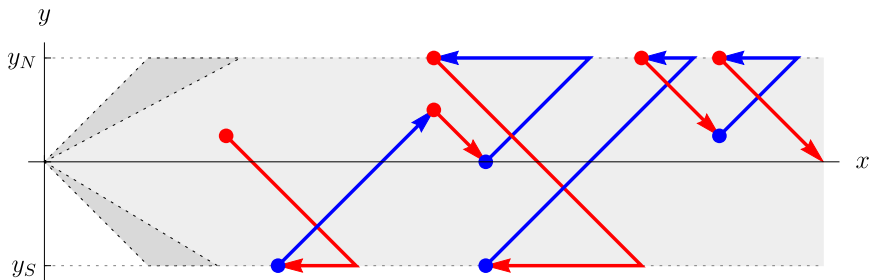
### Question

*What is  $\Pr[\text{kludge}]$ ?*

## When does kludge occur?

Outside attracting basin,

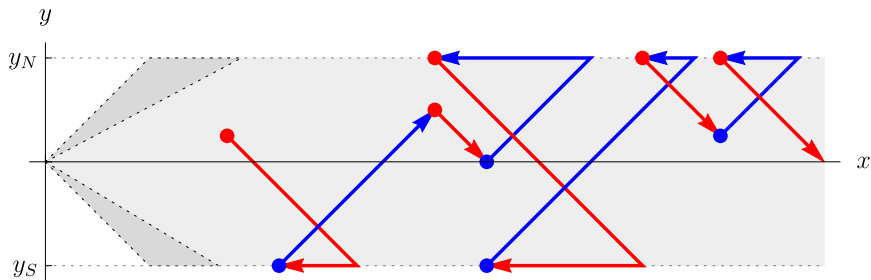
- If  $y(t) = y_N$  or  $y_S$ , then complexity decreases:  $\dot{x}(t) \approx -\gamma$
- If  $y_S < y(t) < y_N$ , then complexity increases:  $\dot{x}(t) = \gamma$



## When does kludge occur?

Then (intuitively)

- Kludge only if policy spends more time *between* than *at* ideals
- i.e., kludge only if  $\dot{x}(t) > 0$  “on average”



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- Kludge only if policy spends more time *between* than *at* ideals
- i.e., kludge only if  $\dot{x}(t) > 0$  “on average”

### Lemma

$\Pr[\textit{kludge}] > 0$  iff

- *initial policy is outside sink, and*
- *“average long-run drift” is asymptotically positive:*

$$\mathbb{E} \left[ \underbrace{\lim_{\tau \rightarrow \infty}}_{\text{long-run}} \underbrace{\lim_{x(0) \rightarrow \infty}}_{\text{asymptotic}} \frac{1}{\tau} \int_0^{\tau} \dot{x}(t) dt \right] > 0$$

# Comparative Statics

## Definition

$$\phi = \frac{1}{\lambda_N - \lambda_S} \ln \frac{\lambda_S (3\lambda_N - \lambda_S)}{\lambda_N (3\lambda_S - \lambda_N)}$$

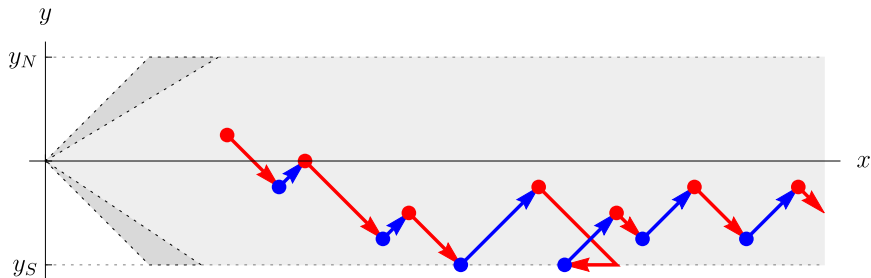
## Theorem

$\Pr[\textit{kludge}] > 0$  iff the following conditions hold:

- *Players' ideals are far apart, and frictions are high:  $y_N - y_S > \gamma/\phi$*
- *Power is relatively equal:  $\frac{1}{3} < \frac{\lambda_I}{\lambda_{-I}} < 3$*
- *Initial policy outside attraction basin*

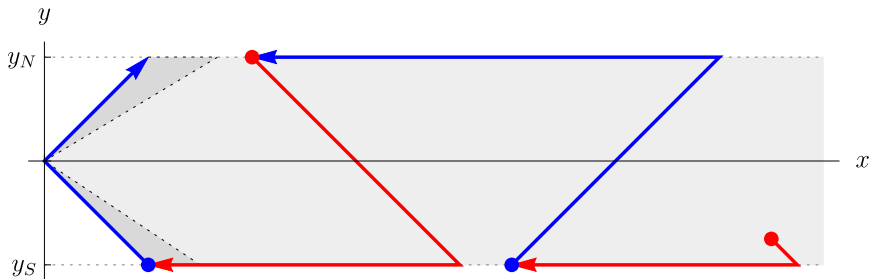
# Institutions matter

- **High** institutional frictions ( $\gamma$ )  $\Rightarrow$  **more** kludge
- \* e.g., supermajority elements, multiple veto points



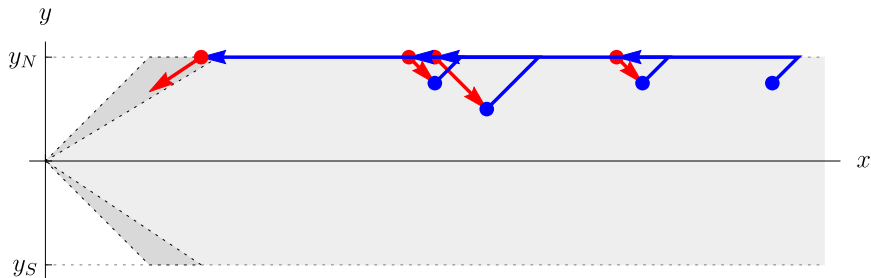
# Institutions matter

- **Low** institutional frictions ( $\gamma$ )  $\Rightarrow$  **less** kludge



# Institutions matter

- Power imbalance (large  $|\lambda_I/\lambda_{-I}|$ )  $\Rightarrow$  kludge  $\downarrow$
- \* Less kludge with one dominant party or with autocracy;
- \* More kludge with democracy



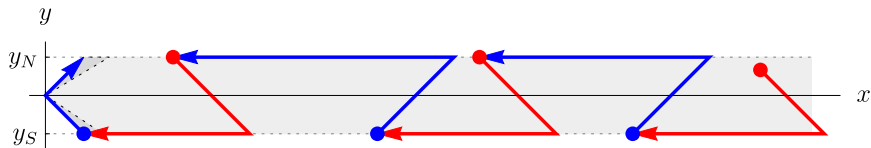


# Institutions matter

- Planner who chooses  $\gamma, \lambda_N, \lambda_S$  faces tradeoff:
  - \* Low-friction, autocratic systems produce less kludge (low  $y(\tau)$ )
  - \* but also more extreme outcomes (high  $|x(\tau)|$ )
- Comparison: US versus Singapore?

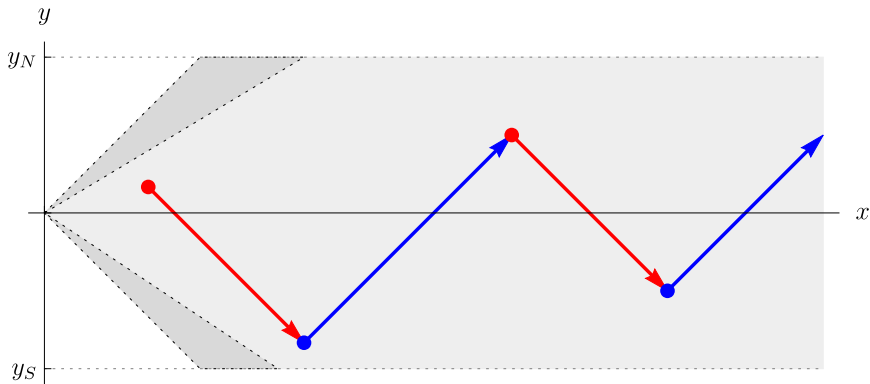
# Ideology / preferences matter

- **Less** extreme competing ideologies (**small**  $y_N - y_S$ )  $\Rightarrow$  **less** kludge



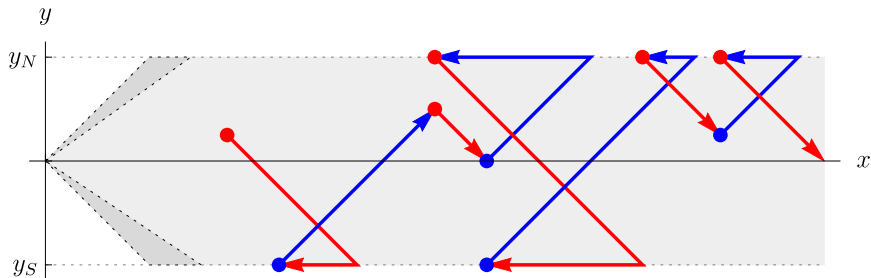
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- **More** extreme competing ideologies (**large**  $y_N - y_S$ )  $\Rightarrow$  **more** kludge



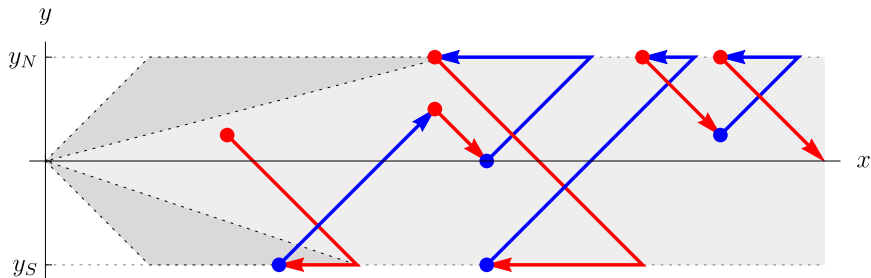
# Ideology / preferences matter

- **Stronger** preferences over ideology (**large**  $\zeta_N, \zeta_S$ )  $\Rightarrow$  **more** kludge:



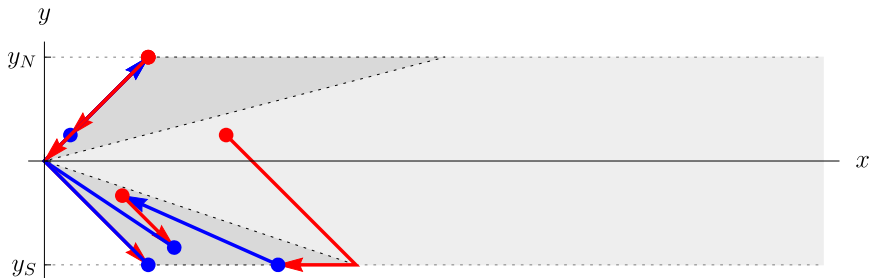
# Ideology / preferences matter

- **Weaker** preferences over ideology (**small**  $\zeta_N, \zeta_S$ )  $\Rightarrow$  **less** kludge:



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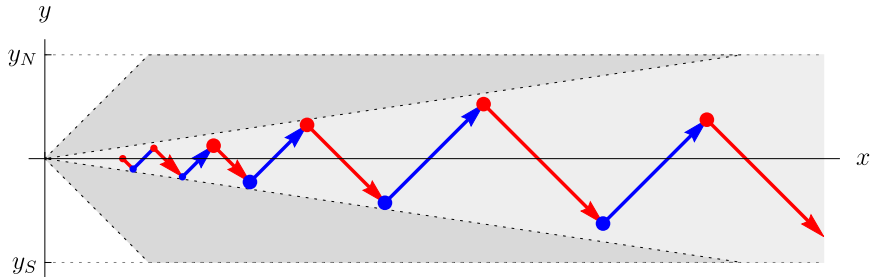


# Complexity begets complexity

## Proposition

Suppose the conditions from the theorem are satisfied, so  $\Pr[\textit{kludge}] > 0$ .

- As  $x(0) \rightarrow \infty$ ,  $\Pr[\textit{kludge}] \rightarrow 1$  uniformly for all  $y(0)$ .
- As  $x(0) \rightarrow 0$ ,  $\Pr[\textit{kludge}] \rightarrow 0$  uniformly for all  $y(0)$ .



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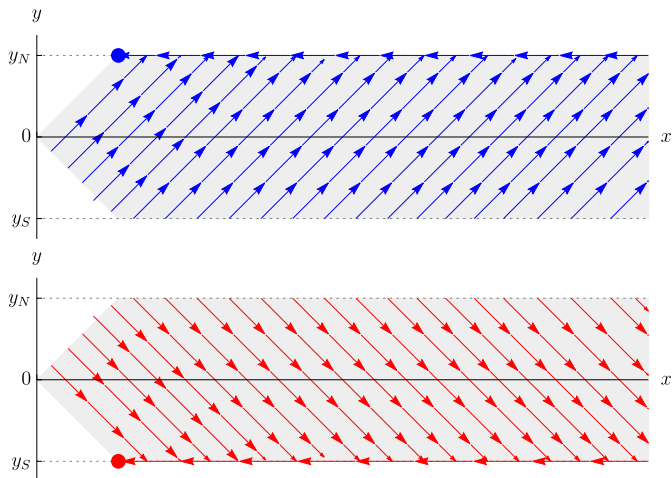


# Modeling Strategic Effects

- Consider nonmyopic players,  $\rho < \infty$
- Markov-perfect equilibria (no punishment schemes)
- Player  $N$  is zealous:  $\zeta_N$  large
- $N$ 's strategic behavior vs: (i) zealous  $S$ , (ii) moderate  $S$

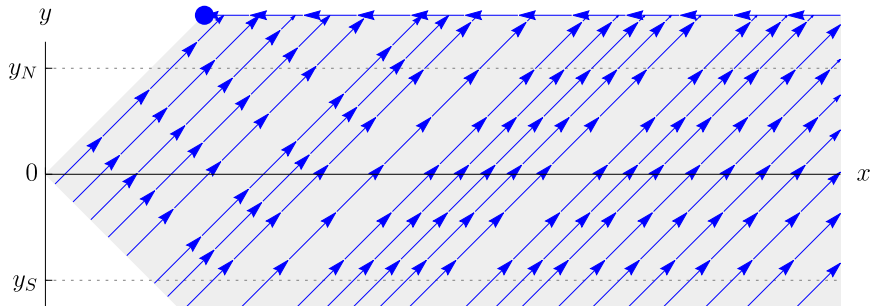
# Zealot vs. Zealot

- Simplifying assumption:  $\zeta_N, \zeta_S \rightarrow \infty$
- Baseline: absent strategic interaction ( $\rho = \infty$ ),

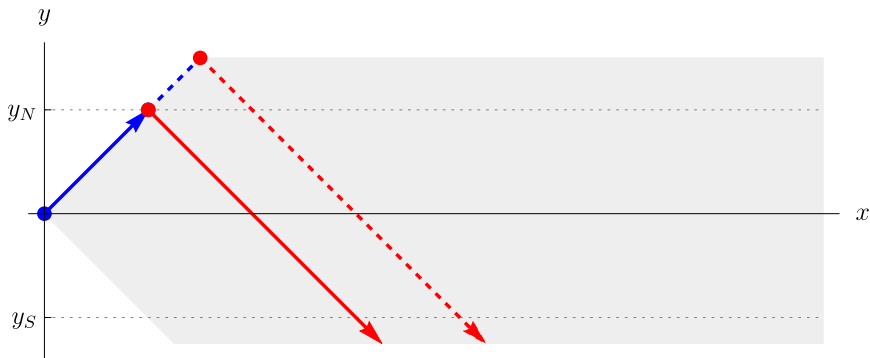


# Strategic Extremism

Zealots “overshoot” ideal.



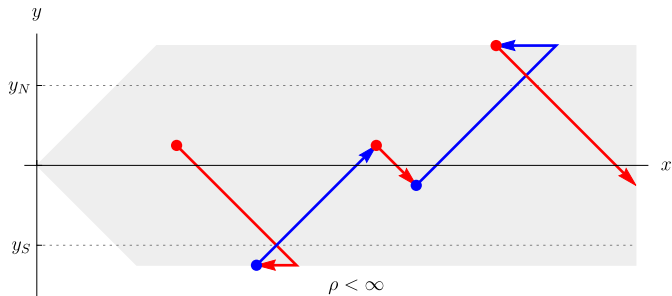
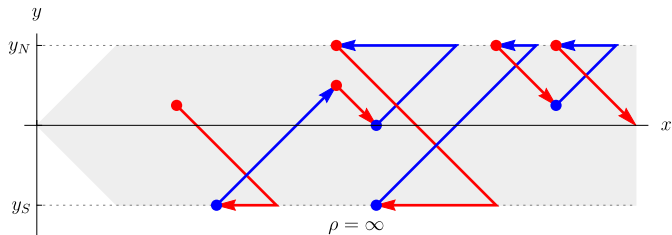
# Shifting the Goalposts



strategy	short run	medium run	longer run
overshoot	away from ideal	<b>closer to ideal</b>	higher complexity
stagnate	<b>at ideal</b>	further from ideal	<b>lower complexity</b>

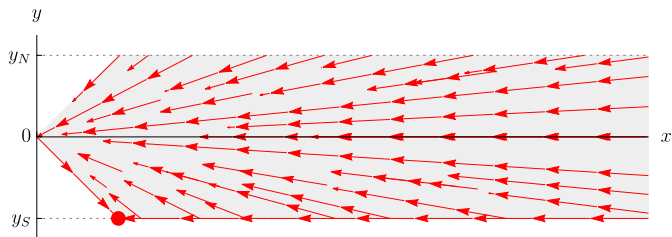
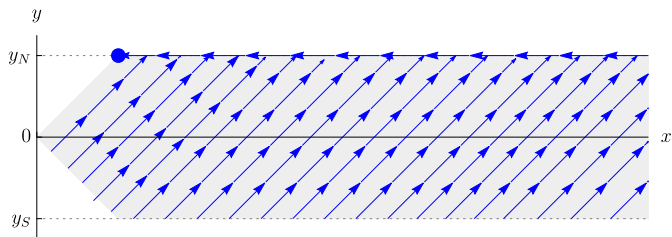
# Strategic extremism $\rightarrow$ more kludge

With zealous players, 'endogenous extremism'



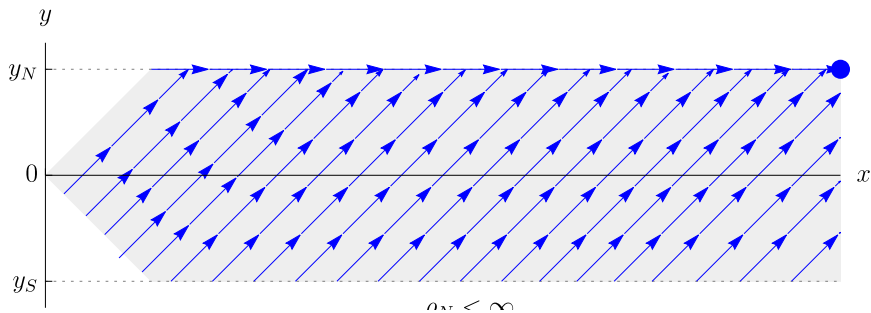
## Zealot vs. Moderate

- Simplifying assumption:  $\zeta_N \rightarrow \infty$  and  $\zeta_S \rightarrow 1$
- \* Also,  $1/\lambda_N \gg 0$
- Baseline: absent strategic interaction ( $\rho = \infty$ ),

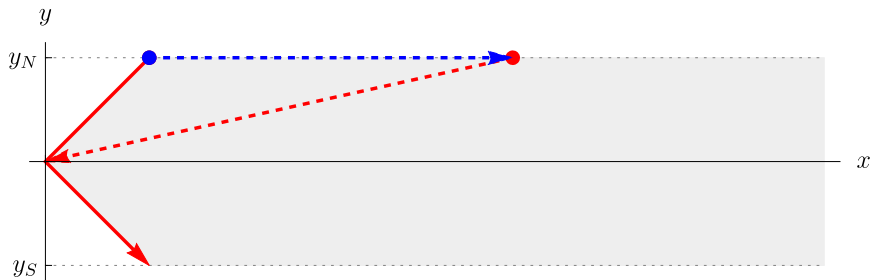


# Intentional Complexity

Zealots add “useless” complexity vs. moderates



# Building a Moat



strategy	short run	medium run	longer run
overshoot	higher complexity	<b>closer to ideal</b>	-
stagnate	<b>lower complexity</b>	further from ideal	-



# Obstructionism

How to protect policy? Depends on opponent:

- *Strategic extremism* vs. zealots
- *Intentional complexity* vs. moderates
- Intentional complexity is transient, strategic extremism is persistent

Long-run effects differ:

- Strategic extremism is *persistent*
- Intentional complexity is *transient*

# Conclusion

- Model of policymaking w/ two key features: complexity and interdependence.
- Highlights role of political conflict in persistent policy inefficiencies
- Implications for optimal institutional design
- OE applications: bureaucracies, routines